

1. Determine whether the following statements are True or False. If False, provide a description (or theorem or picture or counterexample...) that explains your position.
 - A) If $y=f(x)$ is increasing and differentiable and $\Delta x > 0$, then $\Delta y > dy$.
 - B) The sum of two increasing functions is increasing.
 - C) If f_1 is concave up and f_2 is concave down on an interval I , then $f_1 f_2$ is neither concave up nor concave down on I .
2. Let $t(x)=\tan x$ and notice that $t(0)=t(\pi)=0$. Does there exist a number w for which $t'(w)=0$? Why or why not?
3. Consider the function $h(t)=t-2\sin t$ on the interval $[0,2\pi]$. Find all critical numbers of h , state the intervals of increase/decrease, and find all relative extrema.
4. Consider the function $f(x)=x/x^2+1$. State the intervals where the graph is concave upward/downward and find all points of inflection, if applicable.
5. The side of a cube is found to be 10cm long. From this, you find the volume of the cube is $10^3=1000\text{cm}^3$. If your original measurement of the side is accurate to within 2%, approximately how accurate is your calculation of volume?
6. A box with a square base is constructed so the length of one side of the base plus the height is 10 inches. What is the largest possible volume of such a box?
7. Give a **full analysis** of the function $y=x^3+3x^2+1$. Include intercepts (approximate if necessary), asymptotes, intervals of increase/decrease, extrema, intervals of concavity, points of inflection, and a sketch. Note: some of this info may not apply to this function.